



# CS211

# Advanced Computer Architecture

## L06 Memory I

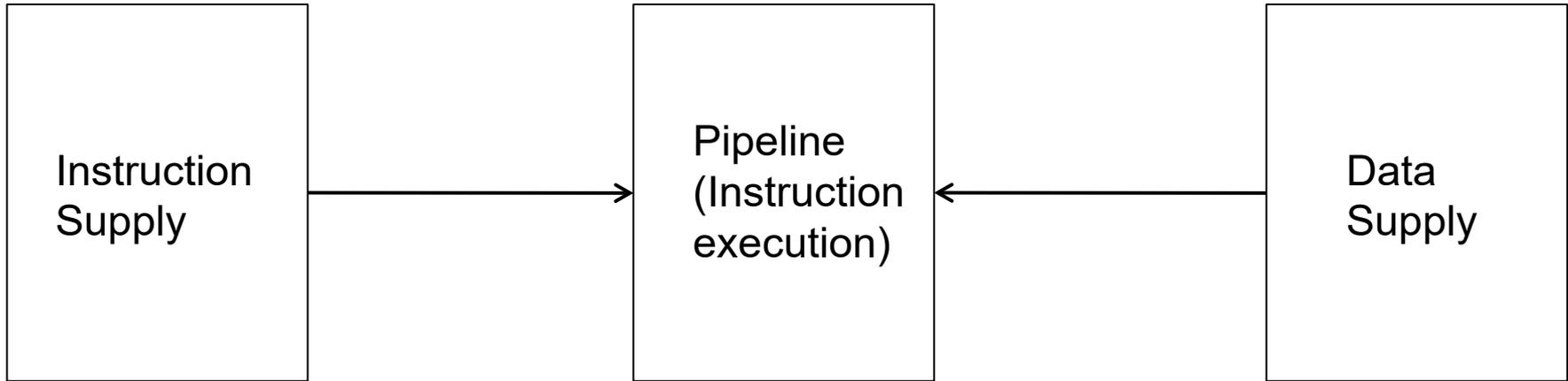
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September 27th, 2020

# Before 1st October

- Quiz 2
  - Today!
  - To collect a slip of questions from TA in the break
  - To submit it to TA at the end of today's class
- HW 1
  - Due at 23:59:59 (UTC+8), Monday, 28th September, 2020
  - Submitted to **Gradescope**
- Paper reading 1
  - Due at 23:59:59 (UTC+8), Monday, 12th October, 2020
- Tomorrow
  - Paper reading 3, HW 2, and Lab 1



# A perfect world

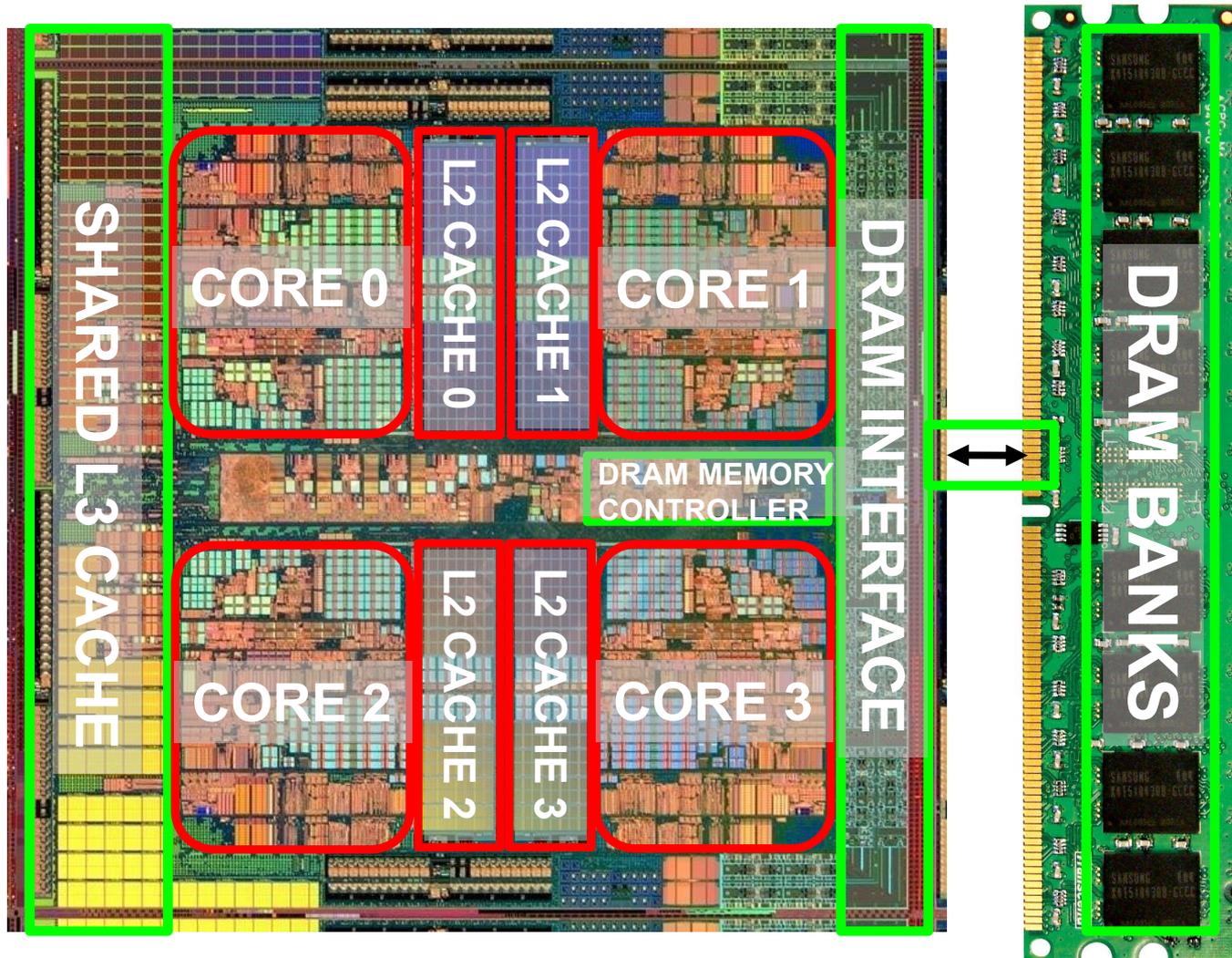


- Zero-cycle latency
- Infinite capacity
- Zero cost
- Perfect control flow

- No pipeline stalls
- Perfect data flow (reg/memory dependencies)
- Zero-cycle interconnect (operand communication)
- Enough functional units
- Zero latency compute

- Zero-cycle latency
- Infinite capacity
- Infinite bandwidth
- Zero cost

# Memory in a Modern System





# Ideal Memory

- Zero access time (latency)
- Infinite capacity
- Zero cost
- Infinite bandwidth (to support multiple accesses in parallel)



# The Problem

- Ideal memory's requirements oppose each other
- Bigger is slower
  - Bigger → Takes longer to determine the location
- Faster is more expensive
  - Memory technology: SRAM vs. DRAM
- Higher bandwidth is more expensive
  - Need more banks, more ports, higher frequency, or faster technology



# DRAM vs. SRAM

- DRAM

- Slower access (capacitor)
- Higher density (1 Transistor/1 Capacitor, 1T-1C cell)
- Lower cost
- Requires refresh (power, performance, circuitry)
- Manufacturing requires putting capacitor and logic together

- SRAM

- Faster access (no capacitor)
- Lower density (6-Transistor cell)
- Higher cost
- No need for refresh
- Manufacturing compatible with logic process (no capacitor)



# The Problem

- **Bigger is slower**
  - SRAM, 512 Bytes, sub-nanosec
  - SRAM, KByte~MByte, ~nanosec
  - DRAM, Gigabyte, ~50 nanosec
  - Hard Disk, Terabyte, ~10 millisec
- **Faster is more expensive (dollars and chip area)**
  - SRAM, < 10\$ per Megabyte
  - DRAM, < 1\$ per Megabyte
  - Hard Disk < 1\$ per Gigabyte
  - These sample values scale with time
- Other technologies have their place as well
  - Flash memory, Intel Optane memory, STT-MRAM, ReRAM, etc.



# Why Memory Hierarchy?

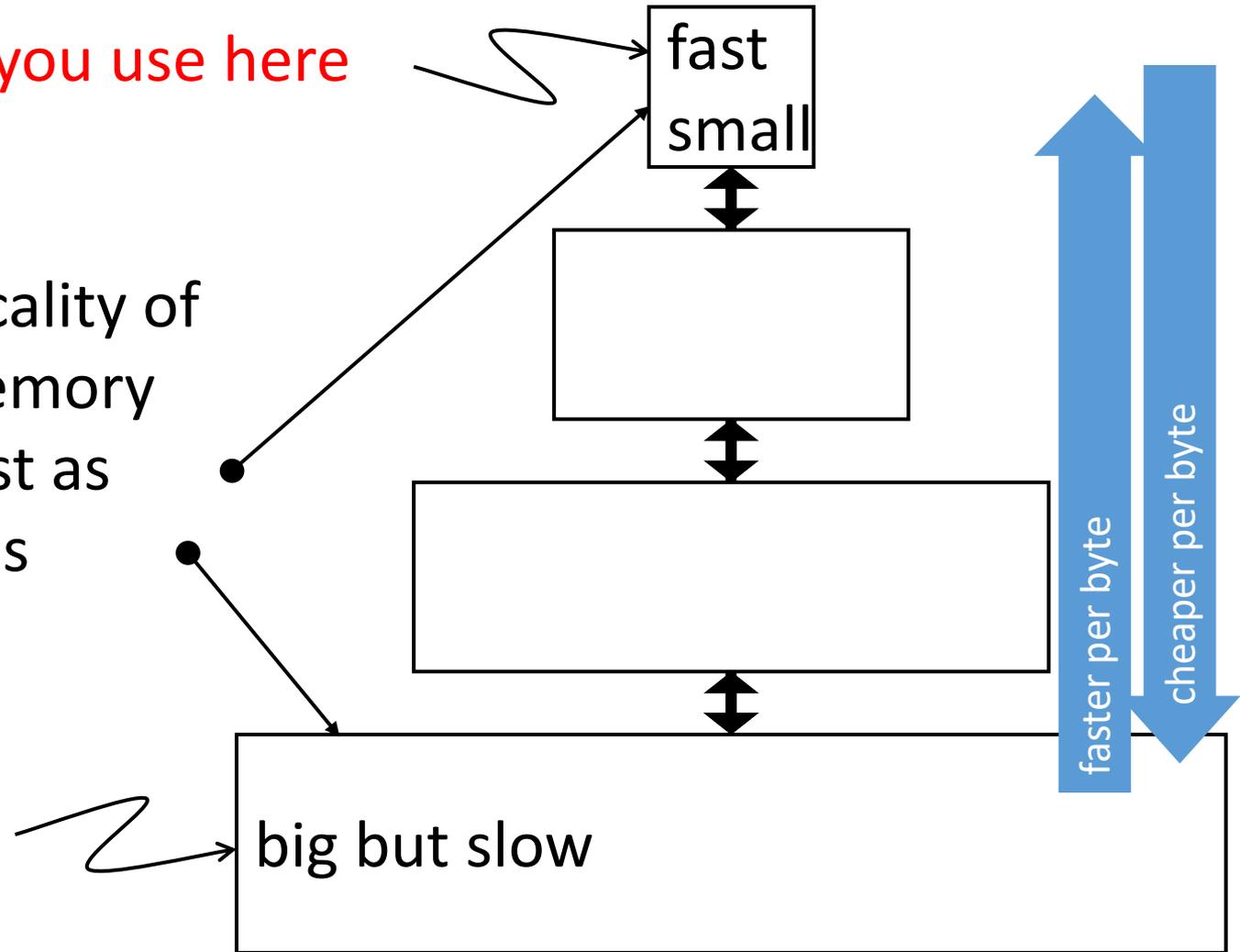
- We want both fast and large
- But we cannot achieve both with a single level of memory
- Idea: **Have multiple levels of storage** (progressively bigger and slower as the levels are farther from the processor) and **ensure most of the data the processor needs is kept in the fast(er) level(s)**

# The Memory Hierarchy

move what you use here

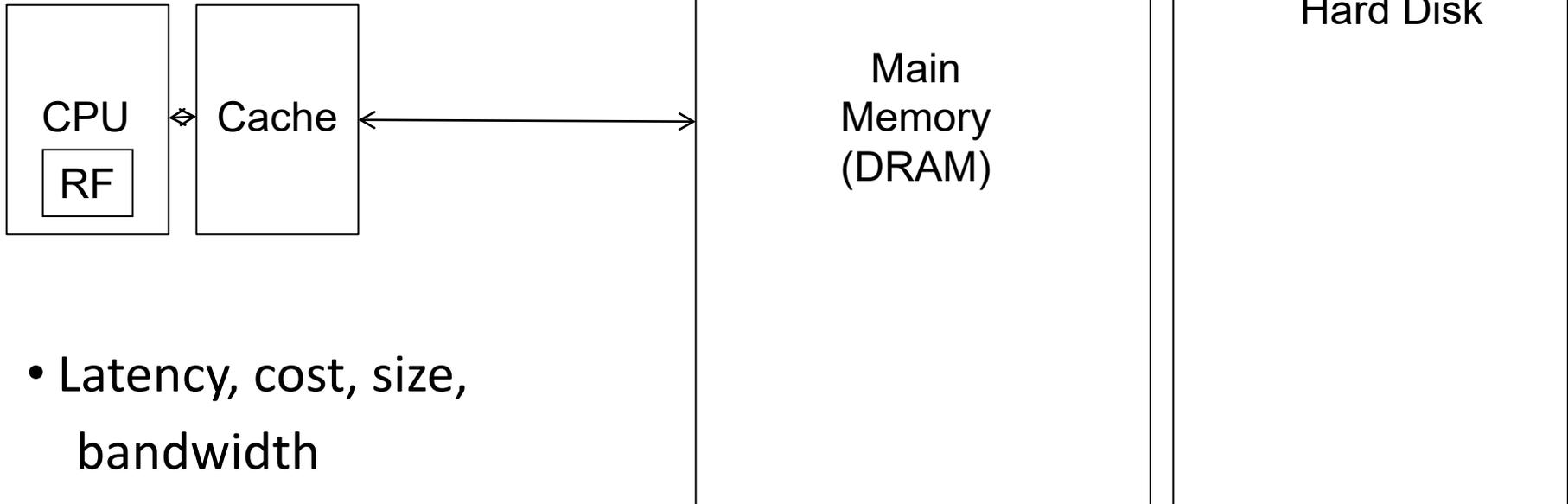
With good locality of reference, memory appears as fast as and as large as

backup everything here



# Memory Hierarchy

- Fundamental tradeoff
  - Fast memory: small
  - Large memory: slow
- Idea: **Memory hierarchy**



- Latency, cost, size, bandwidth



# Locality

- One's recent past is a very good predictor of his/her near future.
- **Temporal Locality**: If you just did something, it is very likely that you will do the same thing again soon
  - since you are here today, there is a good chance you will be here again and again regularly
- **Spatial Locality**: If you did something, it is very likely you will do something similar/related (in space)
  - every time I find you in this room, you are probably sitting close to the same people



# Memory Locality

- A “typical” program has a lot of locality in memory references
  - typical programs are composed of “loops”
- **Temporal**: A program tends to reference the same memory location many times and all within a small window of time
- **Spatial**: A program tends to reference a cluster of memory locations at a time
  - most notable examples:
    - 1. instruction memory references
    - 2. array/data structure references



# Caching Basics: Exploit Temporal Locality

- Idea: Store recently accessed data in automatically managed fast memory (called cache)
- Anticipation: the data will be accessed again soon
- Temporal locality principle
  - Recently accessed data will be again accessed in the near future
  - This is what Maurice Wilkes had in mind:
    - Wilkes, “Slave Memories and Dynamic Storage Allocation,” IEEE Trans. On Electronic Computers, 1965.
    - “The use is discussed of a fast core memory of, say 32000 words as a slave to a slower core memory of, say, one million words in such a way that in practical cases the effective access time is nearer that of the fast memory than that of the slow memory.”

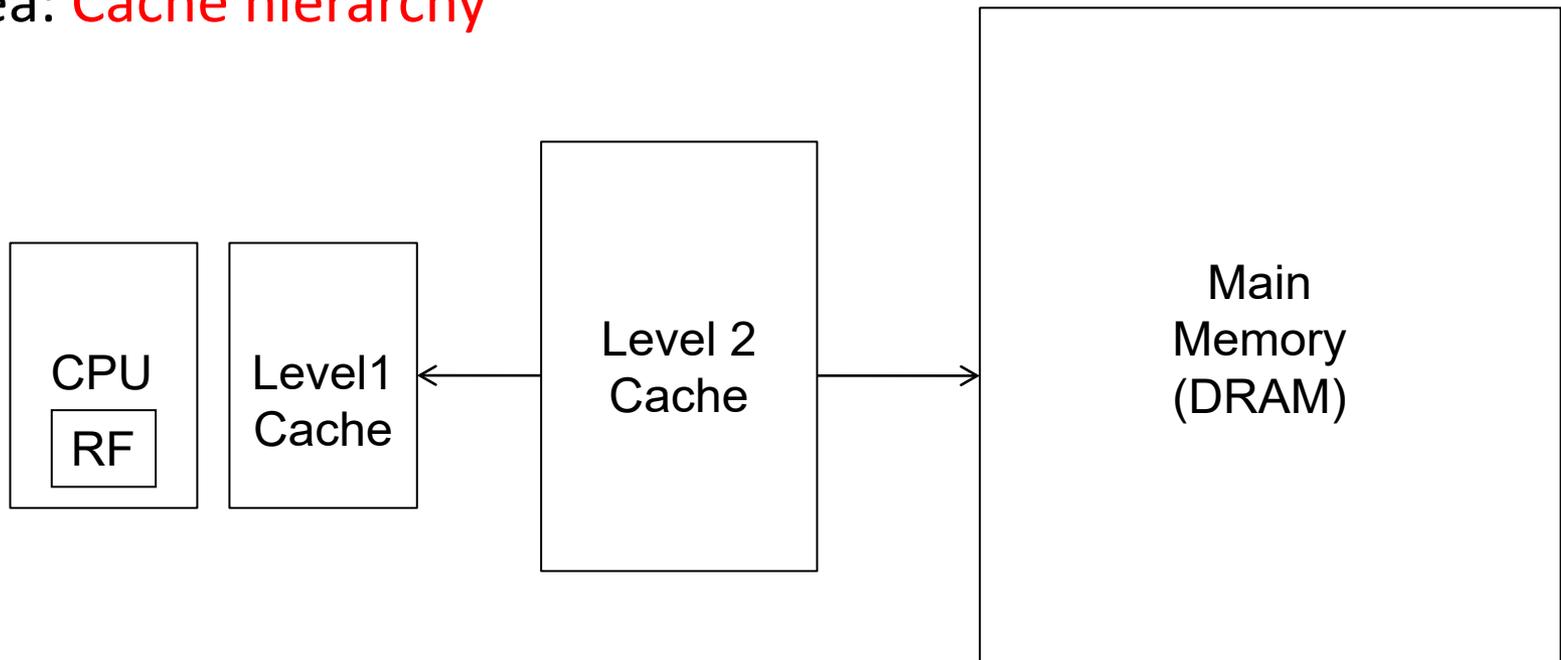


# Caching Basics: Exploit Spatial Locality

- Idea: **Store addresses adjacent to the recently accessed one in automatically managed fast memory**
  - Logically divide memory into equal size blocks
  - Fetch to cache the accessed block in its entirety
- Anticipation: **nearby data will be accessed soon**
- **Spatial locality** principle
  - **Nearby data in memory will be accessed in the near future**
    - E.g., sequential instruction access, array traversal
  - This is what IBM 360/85 implemented
    - 16 Kbyte cache with 64 byte blocks
    - Liptay, “**Structural aspects of the System/360 Model 85 II: the cache,**” IBM Systems Journal, 1968.

# Caching in a Pipelined Design

- The cache needs to be tightly integrated into the pipeline
  - Ideally, access in 1-cycle so that dependent operations do not stall
- High frequency pipeline → Cannot make the cache large
  - But, we want a large cache AND a pipelined design
- Idea: **Cache hierarchy**



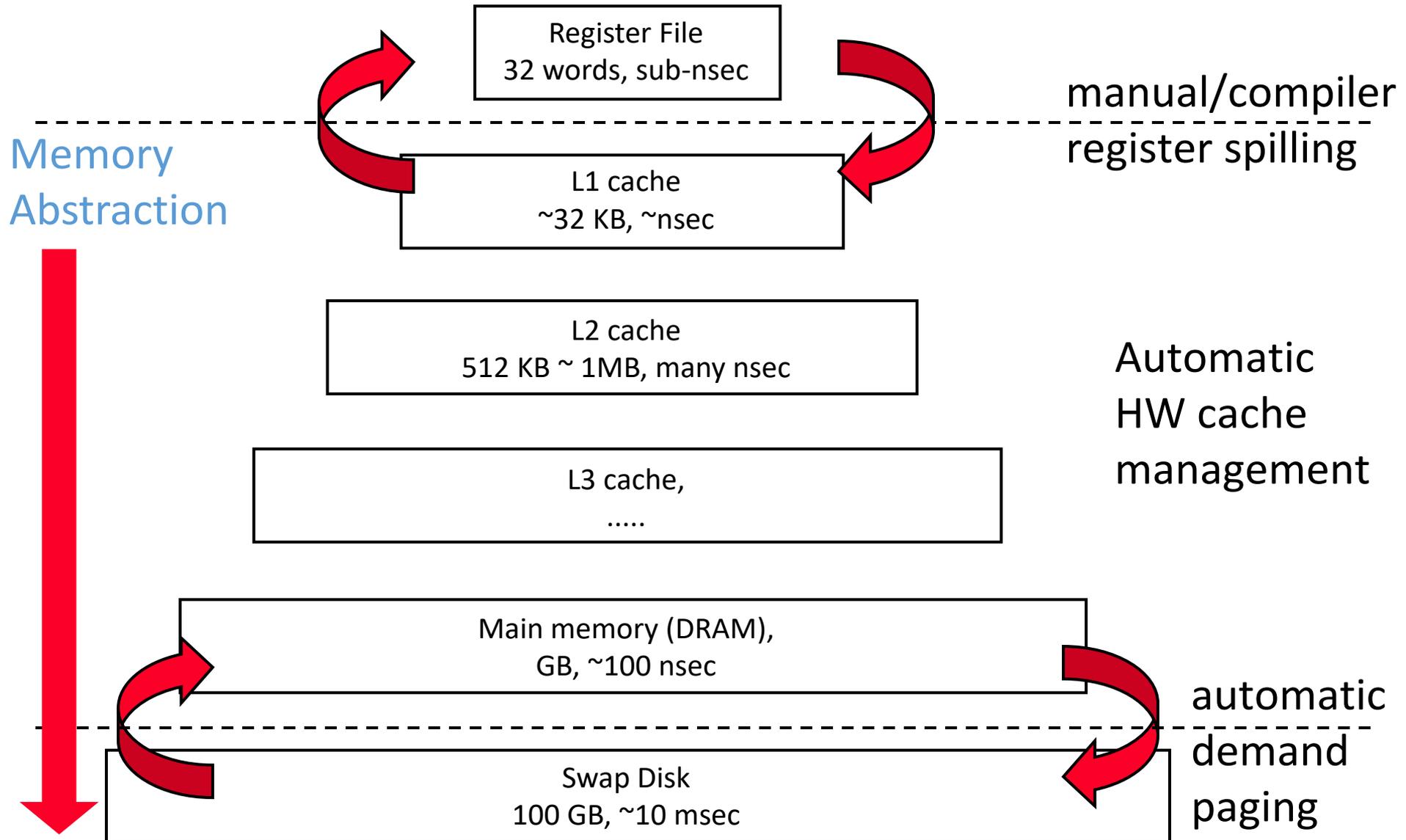


# A Note on Manual vs. Automatic Management

- **Manual:** Programmer manages data movement across levels
  - too painful for programmers on substantial programs
  - Magnetic “core” vs “drum” memory in the 50’s
  - still done in some embedded processors (on-chip scratch pad SRAM in lieu of a cache)
- **Automatic:** Hardware manages data movement across levels, transparently to the programmer
  - ++ programmer’s life is easier
  - simple heuristic: keep most recently used items in cache
  - the average programmer doesn’t need to know about it
    - You don’t need to know how big the cache is and how it works to write a “correct” program! (What if you want a “fast” program?)



# A Modern Memory Hierarchy





# Hierarchical Latency Analysis

- For a given memory hierarchy level  $i$  it has a technology-intrinsic access time of  $t_i$ . The perceived access time  $T_i$  is longer than  $t_i$
- Except for the outer-most hierarchy, when looking for a given address there is
  - a chance (hit-rate  $h_i$ ) you “hit” and access time is  $t_i$
  - a chance (miss-rate  $m_i$ ) you “miss” and access time  $t_i + T_{i+1}$
  - $h_i + m_i = 100\%$

- Thus

$$T_i = h_i \cdot t_i + m_i \cdot (t_i + T_{i+1})$$

$$T_i = t_i + m_i \cdot T_{i+1}$$

keep in mind,  $h_i$  and  $m_i$  are defined to be the hit-rate and miss-rate, respectively, of just the references that missed at  $L_{i-1}$



# Hierarchy Design Considerations

- Recursive latency equation

$$T_i = t_i + m_i \cdot T_{i+1}$$

- The goal: achieve desired  $T_1$  within allowed cost
- $T_i \approx t_i$  is desirable
- Keep  $m_i$  low
  - increasing capacity  $C_i$  lowers  $m_i$ , but beware of increasing  $t_i$
  - lower  $m_i$  by smarter management (replacement::anticipate what you don't need, prefetching::anticipate what you will need)
- Keep  $T_{i+1}$  low
  - faster lower hierarchies, but beware of increasing cost
  - introduce intermediate hierarchies as a compromise



# Intel Pentium 4 Example

- 90nm P4, 3.6 GHz
  - L1 D-cache
    - $C_1 = 16K$
    - $t_1 = 4 \text{ cyc int} / 9 \text{ cycle fp}$
  - L2 D-cache
    - $C_2 = 1024 \text{ KB}$
    - $t_2 = 18 \text{ cyc int} / 18 \text{ cyc fp}$
  - Main memory
    - $t_3 = \sim 50\text{ns or } 180 \text{ cyc}$
  - Notice
    - best case latency is not 1
    - worst case access latencies are into 500+ cycles
- if  $m_1=0.1, m_2=0.1$   
 $T_1=5.8, T_2=36$
- if  $m_1=0.01, m_2=0.01$   
 $T_1=4.2, T_2=19.8$
- if  $m_1=0.05, m_2=0.01$   
 $T_1=5.00, T_2=19.8$
- if  $m_1=0.01, m_2=0.50$   
 $T_1=5.08, T_2=108$



# Cache

- Generically, any structure that “memoizes” frequently used results to avoid repeating the long-latency operations required to reproduce the results from scratch, e.g., a web cache
- Most commonly, an automatically-managed memory hierarchy based on SRAM
  - memoize in SRAM the most frequently accessed DRAM memory locations to avoid repeatedly paying for the DRAM access latency



# Caching Basics

## ■ Block (line): Unit of storage in the cache

- Memory is logically divided into cache blocks that map to locations in the cache

## ■ When data referenced

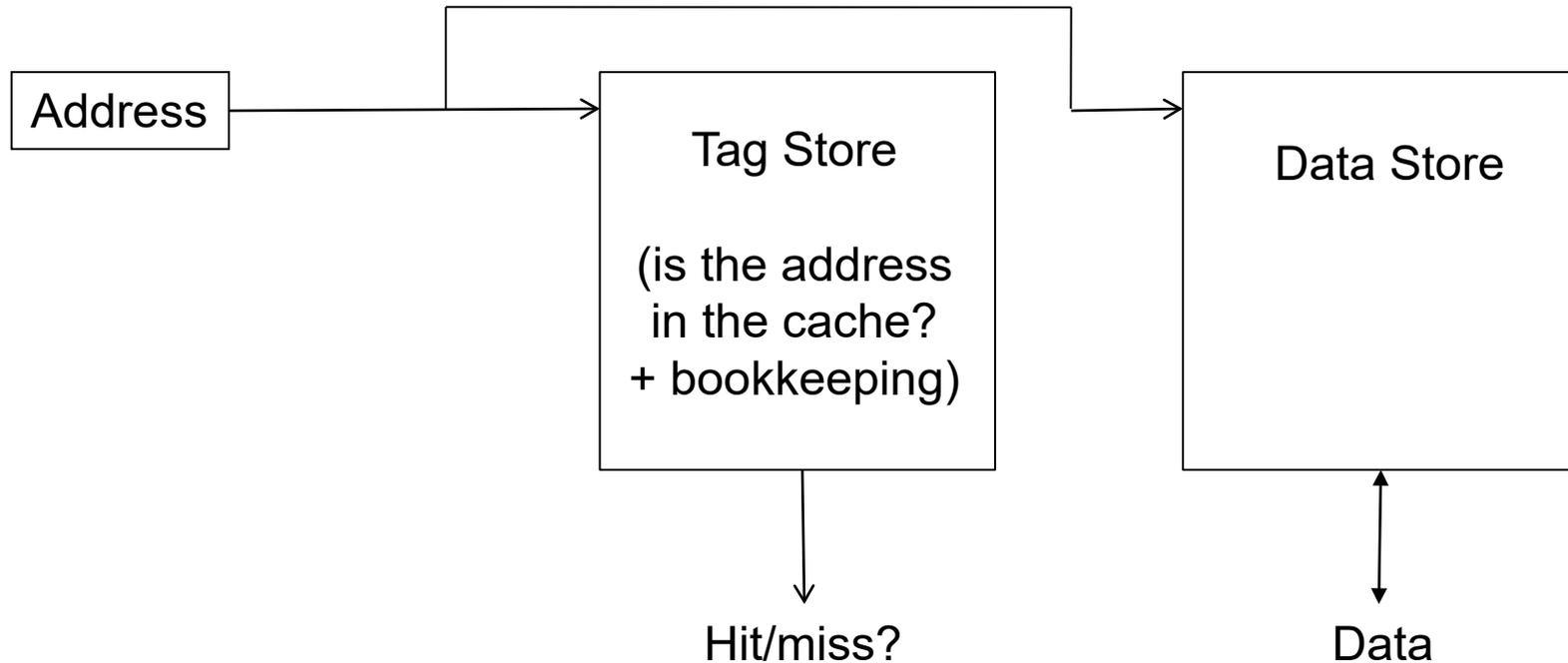
- HIT: If in cache, use cached data instead of accessing memory
- MISS: If not in cache, bring block into cache
  - Maybe have to kick something else out to do it

## ■ Some important cache design decisions

- Placement: where and how to place/find a block in cache?
- Replacement: what data to remove to make room in cache?
- Granularity of management: large, small, uniform blocks?
- Write policy: what do we do about writes?
- Instructions/data: Do we treat them separately?



# Cache Abstraction and Metrics



- Cache hit rate =  $(\# \text{ hits}) / (\# \text{ hits} + \# \text{ misses}) = (\# \text{ hits}) / (\# \text{ accesses})$
- Average memory access time (AMAT)  
=  $(\text{hit-rate} * \text{hit-latency}) + (\text{miss-rate} * \text{miss-latency})$
- *Aside: Can reducing AMAT reduce performance?*

# Associativity in L02

9527 

## Direct mapped

(Block address) % (# of blocks in cache)

$$9527 \% 8 = 7$$

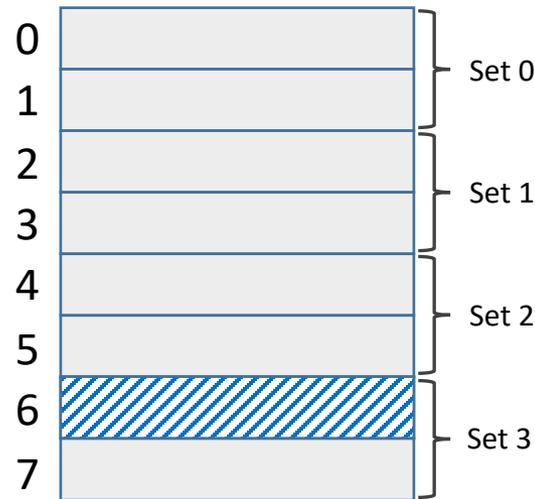


## Set associative

Cache partitioned into multiple sets  
A block can be placed in anywhere in a set

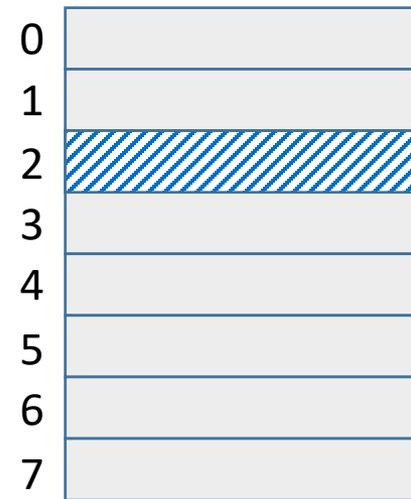
$$9527 \% 4 = 3$$

Four sets, two ways



## Fully associative

A block can be placed anywhere in the cache



A direct mapped cache can be viewed as a set associative cache with  $N$  sets and one way.  
A fully associative cache can be viewed as set associative cache with one set and  $N$  ways.



# Replacement

- How do we choose victim?
  - Verbs: Victimize, evict, replace, cast out
- Many policies are possible
  - FIFO (first-in-first-out)
  - LRU (least recently used), pseudo-LRU
  - LFU (least frequently used)
  - NMRU (not most recently used)
  - NRU
  - Pseudo-random
  - Optimal
  - ...



# Optimal Replacement Policy?

- Evict block with longest reuse distance
  - i.e., next reference to block is farthest in future
  - Requires knowledge of the future
- Can't build it, but can model it with trace
  - Process trace in reverse
- Useful, since it reveals opportunity
  - (X,A,B,C,D,X): LRU 4-way set-associative cache, 2<sup>nd</sup> X will miss

Rabin A. Sugumar, Santosh G. Abraham. Efficient Simulation of Caches under Optimal Replacement with Applications to Miss Characterization . In Proceedings of the ACM SIGMETRICS Conference on Measurement & Modeling Computer Systems, 1993.



# Implementing LRU

- Idea: Evict the least recently accessed block
- Problem: Need to keep track of access ordering of blocks
- Question: 2-way set associative cache:
  - What do you need to implement LRU?
- Question: 4-way set associative cache:
  - How many different orderings possible for the 4 blocks in the set?
  - How many bits needed to encode the LRU order of a block?
  - What is the logic needed to determine the LRU victim?



# Approximations of LRU

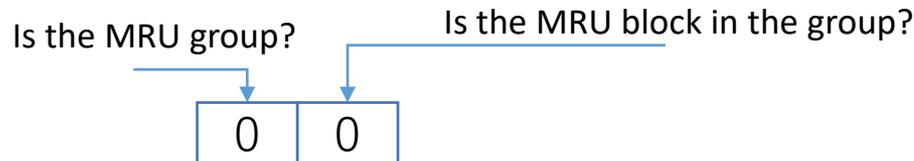
- Most modern processors do not implement “true LRU” in highly-associative caches
- Why?
  - True LRU is complex
  - LRU is an approximation to predict locality anyway (i.e., not the best possible replacement policy)
  - Trashing: temporal reuse exists but LRU fails
    - Reuse distance  $>$  the number of ways in a set
- Examples:
  - **Not MRU** (not most recently used)
    - When the number of ways per set is 2, LRU is equivalent to NMRU
  - **Hierarchical LRU**: divide the 4-way set into 2-way “groups”, track the MRU group and the MRU way in each group
  - **NRU** (Not Recently Used)



# Hierarchical LRU (not MRU)

- Divide a set into multiple groups
- Keep track of the MRU group
- Keep track of the MRU block in each group
- On replacement, select victim as:
  - A not-MRU block in one of the not-MRU groups

4-way cache set, 2 bits





# Not Recently Used (NRU)

- Keep NRU state in 1 bit/block
  - Bit is set to 0 when installed (assume reuse)
  - Bit is set to 0 when referenced (reuse observed)
  - Evictions favor NRU=1 blocks
  - If all blocks are NRU=0
    - Eviction forces all blocks in set to NRU=1
    - Picks one as victim (can be pseudo-random, or rotating, or fixed left-to-right)
  - Simple, similar to virtual memory clock algorithm
  - Provides some scan and thrash resistance
    - Relies on “randomizing” evictions rather than strict LRU order
  - Used by Intel Itanium, SPARC T2
- Variants of NRU
  - NRR: Not Recently Reused: Exploiting reuse locality!
  - RRIP: Re-reference Interval Prediction
    - [Jaleelet al. ISCA 2010]



# Replacement Policy

- LRU vs. Random
  - **Set thrashing**: When the “program working set” in a set is larger than set associativity
  - 4-way: Cyclic references to A, B, C, D, E
    - 0% hit rate with LRU policy
    - Random replacement policy is better when thrashing occurs
- In practice:
  - Depends on workload
  - Average hit rate of LRU and Random are similar
- Hybrid of LRU and Random
  - How to choose between the two? **Set sampling**
    - See Qureshi et al., “**A Case for MLP-Aware Cache Replacement**,” ISCA 2006.



# Aside: Cache versus Page Replacement

- Physical memory (DRAM) is a cache for disk
  - Usually managed by system software via the virtual memory subsystem
- Page replacement is similar to cache replacement
- Page table is the “tag store” for physical memory data store
- What is the difference?
  - Hardware versus software
  - Number of blocks in a cache versus physical memory
  - “Tolerable” amount of time to find a replacement candidate



# What's In a Tag Store Entry?

- Valid bit
- Tag
- Replacement policy bits
  
- Dirty bit?
  - Write back vs. write through caches



# Handling Writes (Stores)

- When do we write the modified data in a cache to the next level?
  - Write through: At the time the write happens
  - Write back: When the block is evicted
  
- Write-back
  - + Can consolidate multiple writes to the same block before eviction
    - Potentially saves bandwidth between cache levels + saves energy
  - Need a bit in the tag store indicating the block is “modified”
  
- Write-through
  - + Simpler
  - + All levels are up to date. **Consistency**: Simpler cache coherence because no need to check lower-level caches
  - More bandwidth intensive; no coalescing of writes



# Handling Writes (Stores)

- Do we allocate a cache block on a write miss?
  - Allocate on write miss: Yes
  - No-allocate on write miss: No
- Allocate on write miss
  - + Can consolidate writes instead of writing each of them individually to next level
  - + Simpler because write misses can be treated the same way as read misses
  - Requires (?) transfer of the whole cache block
- No-allocate
  - + Conserves cache space if locality of writes is low (potentially better cache hit rate)



# Sectored Caches

- Divide a block into subblocks (or sectors)
    - Have separate valid and dirty bits for each sector
    - When is this useful? (Think writes...)
    - How many subblocks do you transfer on a read?
- ++ No need to transfer the entire cache block into the cache  
(A write simply validates and updates a subblock)
- ++ More freedom in transferring subblocks into the cache (a cache block does not need to be in the cache fully)
- More complex design
- May not exploit spatial locality fully when used for reads





# Instruction vs. Data Caches

- Unified:
  - + Dynamic sharing of cache space: no overprovisioning that might happen with static partitioning (i.e., split I and D caches)
  - Instructions and data can thrash each other (i.e., no guaranteed space for either)
  - I and D are accessed in different places in the pipeline. Where do we place the unified cache for fast access?
- First level caches are almost always split
  - Mainly for the last reason above
- Second and higher levels are almost always unified



# Multi-level Caching in a Pipelined Design

- First-level caches (instruction and data)
  - Decisions very much affected by cycle time
  - Small, lower associativity
  - Tag store and data store accessed in parallel
- Second-level caches
  - Decisions need to balance hit rate and access latency
  - Usually large and highly associative; latency not as important
  - Tag store and data store accessed serially
- Serial vs. Parallel access of levels
  - Serial: Second level cache accessed only if first-level misses
  - Second level does not see the same accesses as the first
    - First level acts as a filter



# Conclusion

- Memory hierarchy
- Cache
  - Basics
  - Replacement



# Acknowledgements

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